

Assigned questions for Lecture 10 are listed below (there are two sets). The questions occur in the following editions of “Physical Chemistry” by P.W. Atkins:

10th edition	9th edition	8th edition
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Note: The letter “P” in front of a number indicates that the question is in the “Problem” category as opposed to the “Exercise” category in Atkins’ books. Updates are highlighted in yellow. There are a fair number of differences and missing questions, and unfortunately, a lot of good problems were removed years ago from earlier editions.

Set 1

Question 10.01

3A.3	3.1	3.1
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Slight variation: 10th vs. 8th and 9th Eds.

3.1(a) Calculate the change in entropy when 25 kJ of energy is transferred reversibly and isothermally as heat to a large block of iron at (a) 0°C, (b) 100°C.

3.1(b) Calculate the change in entropy when 50 kJ of energy is transferred reversibly and isothermally as heat to a large block of copper at (a) 0°C, (b) 70°C.

3A.3(a) Calculate the change in entropy when 100 kJ of energy is transferred reversibly and isothermally as heat to a large block of copper at (i) 0 °C, (ii) 50 °C.

3A.3(b) Calculate the change in entropy when 250 kJ of energy is transferred reversibly and isothermally as heat to a large block of lead at (i) 20 °C, (ii) 100 °C.

Question 10.02

3A.7	3.2	3.2
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3.2(a) Calculate the molar entropy of a constant-volume sample of neon at 500 K given that it is 146.22 J K⁻¹ mol⁻¹ at 298 K.

3.2(b) Calculate the molar entropy of a constant-volume sample of argon at 250 K given that it is 154.84 J K⁻¹ mol⁻¹ at 298 K.

Question 10.03

3A.8	3.3	3.3
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3.3(a) Calculate ΔS (for the system) when the state of 3.00 mol of perfect gas atoms, for which $C_{p,m} = (5/2)R$, is changed from 25°C and 1.00 atm to 125°C and 5.00 atm. How do you rationalize the sign of ΔS ?

3.3(b) Calculate ΔS (for the system) when the state of 2.00 mol diatomic perfect gas molecules, for which $C_{p,m} = (7/2)R$, is changed from 25°C and 1.50 atm to 135°C and 7.00 atm. How do you rationalize the sign of ΔS ?

Question 10.04

n/a	3.4	3.4
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Question is missing from 10th Ed.

3.4(a) A sample consisting of 3.00 mol of diatomic perfect gas molecules at 200 K is compressed reversibly and adiabatically until its temperature reaches 250 K. Given that $C_{V,m} = 27.5 \text{ J K}^{-1} \text{ mol}^{-1}$, calculate q , w , ΔU , ΔH , and ΔS .

3.4(b) A sample consisting of 2.00 mol of diatomic perfect gas molecules at 250 K is compressed reversibly and adiabatically until its temperature reaches 300 K. Given that $C_{V,m} = 27.5 \text{ J K}^{-1} \text{ mol}^{-1}$, calculate q , w , ΔU , ΔH , and ΔS .

Set 2**Question 10.05**

3A.9	3.5	3.5
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Slight variations: 10th vs. 8th and 9th Eds.

3.5(a) Calculate ΔH and ΔS_{tot} when two copper blocks, each of mass 10.0 kg, one at 100°C and the other at 0°C, are placed in contact in an isolated container. The specific heat capacity of copper is $0.385 \text{ J K}^{-1} \text{ g}^{-1}$ and may be assumed constant over the temperature range involved.

3.5(b) Calculate ΔH and ΔS_{tot} when two iron blocks, each of mass 1.00 kg, one at 200°C and the other at 25°C, are placed in contact in an isolated container. The specific heat capacity of iron is $0.449 \text{ J K}^{-1} \text{ g}^{-1}$ and may be assumed constant over the temperature range involved.

3A.9(a) Calculate ΔS_{tot} when two copper blocks, each of mass 1.00 kg, one at 50 °C and the other at 0 °C are placed in contact in an isolated container. The specific heat capacity of copper is $0.385 \text{ J K}^{-1} \text{ g}^{-1}$ and may be assumed constant over the temperature range involved.

3A.9(b) Calculate ΔS_{tot} when two iron blocks, each of mass 10.0 kg, one at 100 °C and the other at 25 °C, are placed in contact in an isolated container. The specific heat capacity of iron is $0.449 \text{ J K}^{-1} \text{ g}^{-1}$ and may be assumed constant over the temperature range involved.

Question 10.06

n/a	n/a	n/a
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Missing from 8th and later editions (not sure why).

Ex. 4.9a, 7th edition. Calculate the increase in entropy when 1.00 mol of a monatomic perfect gas with $C_{p,m} = (5/2)R$ is heated from 300 K to 600 K and simultaneously expanded from 30.0 L to 50.0 L.

Ex. 4.9b, 7th edition. Calculate the increase in entropy when 3.50 mol of a monatomic perfect gas with $C_{p,m} = (5/2)R$ is heated from 250 K to 700 K and simultaneously expanded from 20.0 L to 60.0 L.

Question 10.07

n/a	n/a	n/a
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Missing from 8th and later editions (not sure why).

Ex. 4.10a, 7th edition. A system undergoes a process in which the entropy change is $+2.41 \text{ J K}^{-1}$. During the process, 1.00 kJ of heat is added to the system at 500 K. Is the process thermodynamically reversible? Explain your reasoning.

Ex. 4.10b, 7th edition. A system undergoes a process in which the entropy change is $+5.51 \text{ J K}^{-1}$. During the process, 1.50 kJ of heat is added to the system at 350 K. Is the process thermodynamically reversible? Explain your reasoning.

Question 10.08

n/a	n/a	n/a
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Missing from 8th and later editions (not sure why).

Ex. 4.11a, 7th edition. A sample of aluminum of mass 1.75 kg is cooled at constant pressure from 300 K to 265 K. Calculate (a) the energy that must be removed as heat and (b) the change in the entropy of the sample.

Ex. 4.11b, 7th edition. A sample of copper of mass 2.75 kg is cooled at constant pressure from 330 K to 275 K. Calculate (a) the energy that must be removed as heat and (b) the change in the entropy of the sample.

Question 10.09

n/a	n/a	n/a
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Missing from 8th and later editions (not sure why).

Ex. 4.12a, 7th edition. A sample of methane gas of mass 25 g at 250 K and 18.5 atm expands isothermally until the pressure is 2.5 atm. Calculate the change in entropy of the gas.

Ex. 4.12b, 7th edition. A sample of nitrogen gas of mass 35 g at 230 K and 21.1 atm expands isothermally until the pressure is 4.3 atm. Calculate the change in entropy of the gas.

Question 10.10

n/a	n/a	n/a
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Ex. 4.13a, 7th edition. A sample of perfect gas that initially occupies 15.0 L at 250 K and 1.00 atm is compressed isothermally. To what volume must the gas be compressed to reduce its entropy by 5.0 J K^{-1} ?

Ex. 4.13b, 7th edition. A sample of perfect gas that initially occupies 11.0 L at 270 K and 1.20 atm is compressed isothermally. To what volume must the gas be compressed to reduce its entropy by 3.0 J K^{-1} ?

Answer 10.04

n/a	3.4	3.4
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Question is missing from 10th Ed.

E3.4(a) For an adiabatic reversible process, $q = q_{\text{rev}} = \boxed{0}$.

$$\Delta S = \int_i^f \frac{dq_{\text{rev}}}{T} = \boxed{0}$$

$$\begin{aligned} \Delta U &= nC_{V,m}\Delta T [2.16b] = (3.00 \text{ mol}) \times (27.5 \text{ J K}^{-1} \text{ mol}^{-1}) \times (50 \text{ K}) = 4.1 \times 10^3 \text{ J} \\ &= \boxed{+4.1 \text{ kJ}} \end{aligned}$$

$$w = \Delta U \text{ [first law with } q = 0]$$

$$\Delta H = nC_{p,m}\Delta T [2.23b]$$

$$C_{p,m} = C_{V,m} + R [2.26] = (27.5 + 8.3) \text{ J K}^{-1} \text{ mol}^{-1} = 35.8 \text{ J K}^{-1} \text{ mol}^{-1}$$

$$\Delta H = (3.00 \text{ mol}) \times (35.8 \text{ J K}^{-1} \text{ mol}^{-1}) \times (50 \text{ K}) = 5.4 \times 10^3 \text{ J} = \boxed{+5.4 \text{ kJ}}$$

COMMENT. Neither initial nor final pressures and volumes are needed for the solution to this exercise.

E3.4(b) $q = q_{\text{rev}} = 0$ [adiabatic reversible process]

$$\Delta S = \int_i^f \frac{dq_{\text{rev}}}{T} = \boxed{0}$$

$$\begin{aligned} \Delta U &= nC_{V,m}\Delta T = (2.00 \text{ mol}) \times (27.5 \text{ J K}^{-1} \text{ mol}^{-1}) \times (300 - 250) \text{ K} \\ &= 2750 \text{ J} = \boxed{+2.75 \text{ kJ}} \end{aligned}$$

$$w = \Delta U - q = 2.75 \text{ kJ} - 0 = \boxed{2.75 \text{ kJ}}$$

$$\Delta H = nC_{p,m}\Delta T$$

$$C_{p,m} = C_{V,m} + R = (27.5 \text{ J K}^{-1} \text{ mol}^{-1} + 8.314 \text{ J K}^{-1} \text{ mol}^{-1}) = 35.814 \text{ J K}^{-1} \text{ mol}^{-1}$$

$$\text{So } \Delta H = (2.00 \text{ mol}) \times (35.814 \text{ J K}^{-1} \text{ mol}^{-1}) \times (+50 \text{ K}) = 3581.4 \text{ J} = \boxed{3.58 \text{ kJ}}$$

Answer 10.06

n/a	n/a	n/a
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Missing from 8th and later editions (not sure why).

E4.9(a)

$$\Delta S = nC_{V,m} \ln\left(\frac{T_f}{T_i}\right) + nR \ln\left(\frac{V_f}{V_i}\right) \quad [\text{Example 4.3}]$$

$$C_{V,m} = C_{p,m} - R = \frac{5}{2}R - R = \frac{3}{2}R$$

$$\Delta S = (1.00 \text{ mol}) \times \left(\frac{3}{2}\right) \times (8.314 \text{ J K}^{-1} \text{ mol}^{-1}) \ln\left(\frac{600 \text{ K}}{300 \text{ K}}\right)$$

$$+ (1.00 \text{ mol}) \times (8.314 \text{ J K}^{-1} \text{ mol}^{-1}) \times \ln\left(\frac{50.0 \text{ L}}{30.0 \text{ L}}\right) = \boxed{+12.9 \text{ J K}^{-1}}$$

E4.9(b) However the change occurred, ΔS has the same value as if the change happened by reversible heating at constant volume (step 1) followed by reversible isothermal expansion (step 2)

$$\Delta S = \Delta S_1 + \Delta S_2$$

For the first step

$$\Delta S_1 = \int \frac{dq_{\text{rev}}}{T} = \int \frac{C_{V,m} dT}{T} = C_{V,m} \ln \frac{T_f}{T_i} \quad [C_{V,m} = C_{p,m} - R]$$

$$= (3.50 \text{ mol}) \times \left(\frac{3}{2}\right) \times (8.3145 \text{ J K}^{-1} \text{ mol}^{-1}) \times \ln \frac{700 \text{ K}}{250 \text{ K}} = 44.9 \text{ J K}^{-1}$$

and for the second

$$\Delta S_2 = \int \frac{dq_{\text{rev}}}{T} = \frac{q_{\text{rev}}}{T}$$

where $q_{\text{rev}} = -w = \int p dV = nRT \ln \frac{V_f}{V_i}$,

so $\Delta S_2 = nR \ln \frac{p_i}{p_f} = (3.50 \text{ mol}) \times (8.3145 \text{ J K}^{-1} \text{ mol}^{-1}) \times \ln \frac{60.0 \text{ L}}{20.0 \text{ L}} = 32.0 \text{ J K}^{-1}$

$$\Delta S = 44.9 + 32.0 \text{ J K}^{-1} = \boxed{76.9 \text{ J K}^{-1}}$$

Answer 10.07

n/a	n/a	n/a
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Missing from 8th and later editions (not sure why).

$$\mathbf{E4.10(a)} \quad \Delta S = \frac{q_{\text{rev}}}{T} \text{ [constant temperature]}$$

If reversible $q = q_{\text{rev}}$.

$$q_{\text{rev}} = T \Delta S = (500 \text{ K}) \times (2.41 \text{ J K}^{-1}) = 1.21 \text{ kJ}$$

$$1.21 \text{ kJ} \neq 1.00 \text{ kJ} = q$$

Therefore, the process is not reversible.

$$\mathbf{E4.10(b)} \quad \Delta S = \frac{q_{\text{rev}}}{T} \text{ If reversible } q = q_{\text{rev}}$$

$$q_{\text{rev}} = T \Delta S = (5.51 \text{ J K}^{-1}) \times (350 \text{ K}) \\ = 1928.5 \text{ J}$$

$$q = 1.50 \text{ kJ} \neq 19.3 \text{ kJ} = q_{\text{rev}}$$

$q \neq q_{\text{rev}}$; therefore the process is not reversible

Answer 10.08

n/a	n/a	n/a
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Missing from 8th and later editions (not sure why).

E4.11(a) (a) $\Delta H = \int_{T_1}^{T_2} nC_{p,m} dT$ [constant pressure]

$C_{p,m}/(\text{J K}^{-1} \text{ mol}^{-1}) = (a + bT)$ [Table 2.2], $a = 20.67$, $b = 12.38 \times 10^{-3} \text{ K}^{-1}$

$$\Delta H = \int_{T_1}^{T_2} n(a + bT) \text{ J K}^{-1} \text{ mol}^{-1} dT$$

$$= na(T_2 - T_1) \text{ J K}^{-1} \text{ mol}^{-1} + \frac{1}{2}nb(T_2^2 - T_1^2) \text{ J K}^{-1} \text{ mol}^{-1}$$

$$n = \frac{1.75 \times 10^3 \text{ g}}{26.98 \text{ g mol}^{-1}} = 64.8\bar{6} \text{ mol}$$

$$\Delta H = [(64.8\bar{6} \text{ mol}) \times (20.67) \times (265 - 300) \text{ K}$$

$$+ (\frac{1}{2}) \times (64.8\bar{6} \text{ mol}) \times (12.38 \times 10^{-3} \text{ K}^{-1}) \times (265^2 - 300^2) \text{ K}^2] \text{ J K}^{-1} \text{ mol}^{-1}$$

$$\Delta H = -54.9 \times 10^3 \text{ J} = \boxed{-54.9 \text{ kJ}}$$

E4.11(b) (a) The heat flow is

$$q = C_p \Delta T = nC_{p,m} \Delta T$$

$$= \left(\frac{2.75 \text{ kg}}{63.54 \times 10^{-3} \text{ kg mol}^{-1}} \right) \times (24.44 \text{ J K}^{-1} \text{ mol}^{-1}) \times (275 - 330) \text{ K}$$

$$= \boxed{-58.2 \times 10^3 \text{ J}}$$

(b) $\Delta S = \int \frac{dq_{\text{rev}}}{T} = \int \frac{C_p dT}{T} = nC_{p,m} \ln \frac{T_f}{T_i}$

$$= \left(\frac{2.75 \text{ kg}}{63.54 \times 10^{-3} \text{ kg mol}^{-1}} \right) \times (24.44 \text{ J K}^{-1} \text{ mol}^{-1}) \times \ln \frac{275 \text{ K}}{330 \text{ K}} = \boxed{-193 \text{ J K}^{-1}}$$

Answer 10.09

n/a	n/a	n/a
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Missing from 8th and later editions (not sure why).

$$\text{E4.12(a)} \quad \Delta S = nR \ln\left(\frac{V_f}{V_i}\right) \quad [4.17]; \quad \frac{p_i}{p_f} = \frac{V_f}{V_i} \quad [\text{Boyle's law}]$$

$$\Delta S = nR \ln\left(\frac{p_i}{p_f}\right) = \left(\frac{25 \text{ g}}{16.04 \text{ g mol}^{-1}}\right) \times (8.314 \text{ J K}^{-1} \text{ mol}^{-1}) \times \ln\left(\frac{18.5 \text{ atm}}{2.5 \text{ atm}}\right)$$

$$= \boxed{+26 \text{ J K}^{-1}}$$

$$\text{E4.12(b)} \quad \Delta S = \int \frac{dq_{\text{rev}}}{T} = \frac{q_{\text{rev}}}{T} \quad \text{where } q_{\text{rev}} = -w = nRT \ln \frac{V_f}{V_i} = nRT \ln \frac{p_i}{p_f}$$

$$\text{so } \Delta S = nR \ln \frac{p_i}{p_f} = \left(\frac{35 \text{ g}}{28.013 \text{ g mol}^{-1}}\right) \times (8.3145 \text{ J K}^{-1} \text{ mol}^{-1}) \times \ln \frac{21.1 \text{ atm}}{4.3 \text{ atm}} = \boxed{17 \text{ J K}^{-1}}$$

Answer 10.10

n/a	n/a	n/a
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Missing from 8th and later editions (not sure why).

$$\text{E4.13(a)} \quad \Delta S = nR \ln\left(\frac{V_f}{V_i}\right) \quad [4.17]$$

The number of moles (or nR) and then V_f need to be determined

$$nR = \frac{p_i V_i}{T_i} = \frac{(1.00 \text{ atm}) \times (15.0 \text{ L})}{250 \text{ K}} = \frac{(1.013 \times 10^5 \text{ Pa}) \times (15.0 \times 10^{-3} \text{ m}^3)}{250 \text{ K}} = 6.08 \text{ J K}^{-1}$$

$$\ln \frac{V_f}{V_i} = \frac{\Delta S}{nR} = \frac{-5.0 \text{ J K}^{-1}}{6.08 \text{ J K}^{-1}} = -0.823$$

$$\text{Hence, } V_f = V_i e^{-0.823} = (15.0 \text{ L}) \times (0.439) = \boxed{6.6 \text{ L}}$$

$$\text{E4.13(b)} \quad \Delta S = \int \frac{dq_{\text{rev}}}{T} = \frac{q_{\text{rev}}}{T} \quad \text{where } q_{\text{rev}} = -w = nRT \ln \frac{V_f}{V_i}$$

$$\text{so } \Delta S = nR \ln \frac{V_f}{V_i} \quad \text{and } V_f = V_i \exp\left(\frac{\Delta S}{nR}\right)$$

We need to compute the amount of gas from the perfect gas law

$$pV = nRT \quad \text{so } n = \frac{pV}{RT} = \frac{(1.20 \text{ atm}) \times (11.0 \text{ L})}{(0.08206 \text{ L atm K}^{-1} \text{ mol}^{-1}) \times (270 \text{ K})} = 0.596 \text{ mol}$$

$$\text{So } V_f = (11.0 \text{ L}) \exp\left(\frac{-3.0 \text{ J K}^{-1}}{(0.596 \text{ mol}) \times (8.3145 \text{ J K}^{-1} \text{ mol}^{-1})}\right) = \boxed{6.00 \text{ L}}$$

Answers:

Ex. 4.9a, 7th edition

12.9 J K⁻¹

Ex. 4.9b, 7th edition

76.9 J K⁻¹

Ex. 4.10a, 7th edition

not reversible

Ex. 4.10b, 7th edition

not reversible

Ex. 4.11a, 7th edition

(a) -58.2 kJ (b) -193 J K⁻¹

Ex. 4.11b, 7th edition

(a) -54.9 kJ (b) -195 J K⁻¹

Ex. 4.12a, 7th edition

26 J K⁻¹

Ex. 4.12b, 7th edition

17 J K⁻¹

Ex. 4.13a, 7th edition

6.6 L

Ex. 4.13b, 7th edition

6.0 L

A-list answers for the 9th edition:

3.1 (a) 92 J K⁻¹; (b) 67 J K⁻¹

3.2 152.67 J K⁻¹ mol⁻¹

3.3 -22.1 J K⁻¹

3.4 $q = 0$, $\Delta S = 0$, $\Delta U = +4.1$ kJ, $w = +4.1$ kJ, $\Delta H = 5.4$ kJ

3.5 $\Delta H_{\text{tot}} = 0$, $\Delta S_{\text{tot}} = 93.4$ J K⁻¹